#### **VERSION A**

# Midterm Exam – Econ 2400 October 6, 2025 Department of Economics, York University

**Instructions:** On this exam, unless otherwise asked, you should *not* show how you arrived at your answer, only write the answer in the space indicated on the relevant answer sheet. Answers must be given on the correct answer sheet, one for each problem. If you make a mistake, ask for a new answer sheet. Do not fold the answer sheets or write on the back, or outside of the indicated space.

Student name: SID number:

#### Problem 1. Real GDP Growth [4 marks]

Consider an economy with two (final) goods, A and B, and two periods, 1 and 2. The notation is the same as in class. Prices of good A are given by  $P_1^A$  and  $P_2^A$  in periods 1 and 2, respectively, and the corresponding prices of good B are  $P_1^B$  and  $P_2^B$ . Similarly, the quantities of good A equal  $Q_1^A$  and  $Q_2^A$  in each of the two periods, and the quantities of good B are  $Q_1^B$  and  $Q_2^B$ .

We let  $g_1$  and  $g_2$  be the (gross) growth rates in real GDP, using years 1 and 2, respectively, as base years:

$$g_1 = \frac{P_1^A Q_2^A + P_1^B Q_2^B}{P_1^A Q_1^A + P_1^B Q_1^B},$$

and

$$g_2 = \frac{P_2^A Q_2^A + P_2^B Q_2^B}{P_2^A Q_1^A + P_2^B Q_1^B}.$$

Now also assume that the quantities of goods A and B grow at the same rate from period 1 to period 2:

$$\frac{Q_2^A}{Q_1^A} = \frac{Q_2^B}{Q_1^B} = G. (1)$$

We also assume that 0 < G < 1.

- (a) Determine which is true: (1)  $g_1 > g_2$ ; (2)  $g_1 < g_2$ ; (3)  $g_1 = g_2$ ; or (4) it is not possible to say based on the information provided. [1 mark]
- (b) Let  $GDP_2$  denote nominal GDP in period 2. Write an expression for  $GDP_2$  in terms of some, or all, of  $P_1^A$ ,  $P_2^A$ ,  $P_1^B$ ,  $P_2^B$ ,  $Q_1^A$ ,  $Q_2^A$ ,  $Q_1^B$ , and  $Q_2^B$ . [1 mark]

- (c) Write an expression for  $g_1$ . Your answer should be expressed in terms of some (or all) of G,  $P_1^A$ ,  $P_1^B$ ,  $Q_1^A$ , and  $Q_1^B$ , but none of the period-2 prices or quantities. Simplify your answer as much as possible; note the "some-or-all-of" part of the question. [1 mark]
  - (d) Show how you arrived at your answer under (c). [1 mark]

## Problem 2. Growth Rates and Per-Capita GDP [4 marks]

The table below shows some (incomplete) information about the natural logarithms of two macro variables: total GDP,  $Y_t$ ; and total population,  $L_t$ .

t	$ln(Y_t)$	$\ln(L_t)$
1	1.00	0.80
2	1.05	0.90
3		1.00

Let  $y_t = Y_t/L_t$  denote (non-logged) GDP per capita. Also, let  $g_t^Y = \frac{Y_t - Y_{t-1}}{Y_t}$  denote the net growth rate in  $Y_t$ , with analogous notation for the growth rates of  $y_t$  and  $L_t$ .

- (a) Find the natural logarithm of GDP per capita in period 2,  $ln(y_2)$ . [1 mark]
- (b) Find the (approximate) non-logged GDP per capita in period 2,  $y_2$ . [1 mark]
- (c) Find the (approximate) net growth rate in GDP per capita in period 2,  $g_2^y$ . [1 mark]
- (d) Assume that  $g_3^y = 0.10 = 10\%$ . Find the (approximate) non-logged level of total GDP in period 3,  $Y_3$ . [1 mark]

## Problem 3. Business Cycles [4 marks]

- (a) The diagram provided on the answer sheet shows the time path for the percentage deviation from trend in real GDP. In the same diagram, draw another path showing deviations from trend for some other (imagined) macro variable that is (i) counter-cyclical and (ii) coincident with the business cycle. Also indicate the peak of the business cycle in the diagram. (There are multiple peaks, but you only need to indicate one.) [2 marks]
- (b) What do we call the curve that describes the relationship between fluctuations in employment (or GDP) and fluctuations in inflation (or nominal prices or wages)? Hint: it starts with a P. [1 mark]
  - (c) Mention one year in which Canada was in a recession after 1961. [0.5 marks]
- (d) Mention one macro variable that is leading the business cycle in Canadian data. [0.5 marks]

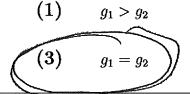
# Econ 2400 Midterm Exam October 6, 2025 – Answer sheet for Problem 1

version A answers

Student Name:

SID Number:

## Answer to 1 (a) (circle one):



- $(2) g_1 < g_2$
- (4) Not possible to say

Answer to 1 (b):

#### Answer to 1 (c):

$$GDP_2 = P_2^A Q_2^A + P_2^B Q_2^B$$

$$g_1 = \mathcal{G}$$

Answer to 1 (d): (show derivation below)

$$g_{1} = \frac{P_{1}^{A} Q_{2}^{A} + P_{1}^{B} Q_{2}^{R}}{P_{1}^{A} Q_{1}^{A} + P_{1}^{B} Q_{1}^{R}}$$

$$= \frac{P_{1}^{A} Q_{1}^{A} + P_{1}^{B} Q_{1}^{R}}{P_{1}^{A} Q_{1}^{A} + P_{1}^{B} Q_{1}^{R}}$$

$$= \frac{G [P_{1}^{A} Q_{1}^{A} + P_{1}^{B} Q_{1}^{R}]}{P_{1}^{A} Q_{1}^{A} + P_{1}^{B} Q_{1}^{R}} = G$$

#### Econ 2400 Midterm Exam October 6, 2025 - Answer sheet for Problem 2

Student Name:

SID Number:

Answer to 2 (a):

$$\ln(y_2) = \emptyset, 15$$

Answer to 2 (b):

$$y_2 = 1,161834$$

Answer to 2 (c):

$$g_2^y = -6.05 = -5\%$$

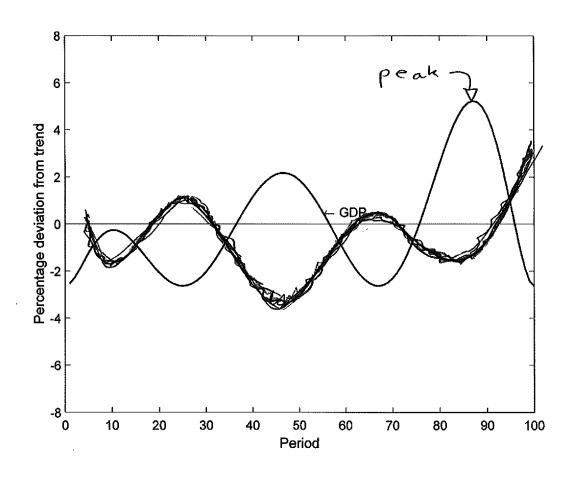
Answer to 2 (d):

$$Y_3 = 3,490343$$

Student	Mana
Student	IVame:

SID Number:

Answer to 3 (a):



Answer to 3 (b):

Answer to 3 (c):

Answer to 3 (d):

Phillips care

2009 (for example) Stock price index

#### **VERSION B**

## Midterm Exam – Econ 2400 October 6, 2025 partment of Economics, York University

Department of Economics, York University

**Instructions:** On this exam, unless otherwise asked, you should *not* show how you arrived at your answer, only write the answer in the space indicated on the relevant answer sheet. Answers must be given on the correct answer sheet, one for each problem. If you make a mistake, ask for a new answer sheet. Do not fold the answer sheets or write on the back, or outside of the indicated space.

Student name: SID number:

## Problem 1. Real GDP Growth [4 marks]

Consider an economy with two (final) goods, A and B, and two periods, 1 and 2. The notation is the same as in class. Prices of good A are given by  $P_1^A$  and  $P_2^A$  in periods 1 and 2, respectively, and the corresponding prices of good B are  $P_1^B$  and  $P_2^B$ . Similarly, the quantities of good A equal  $Q_1^A$  and  $Q_2^A$  in each of the two periods, and the quantities of good B are  $Q_1^B$  and  $Q_2^B$ .

We let  $g_1$  and  $g_2$  be the (gross) growth rates in real GDP, using years 1 and 2, respectively, as base years:

$$g_1 = \frac{P_1^A Q_2^A + P_1^B Q_2^B}{P_1^A Q_1^A + P_1^B Q_1^B},$$

and

$$g_2 = \frac{P_2^A Q_2^A + P_2^B Q_2^B}{P_2^A Q_1^A + P_2^B Q_1^B}.$$

Now also assume that the quantities of goods A and B grow at the same rate from period 1 to period 2:

$$\frac{Q_2^A}{Q_1^A} = \frac{Q_2^B}{Q_1^B} = Z. (1)$$

We also assume that Z > 1.

- (a) Determine which is true: (1)  $g_1 > g_2$ ; (2)  $g_1 < g_2$ ; (3)  $g_1 = g_2$ ; or (4) it is not possible to say based on the information provided. [1 mark]
- (b) Let  $GDP_2$  denote nominal GDP in period 2. Write an expression for  $GDP_2$  in terms of some, or all, of  $P_1^A$ ,  $P_2^A$ ,  $P_1^B$ ,  $P_2^B$ ,  $Q_1^A$ ,  $Q_2^A$ ,  $Q_1^B$ , and  $Q_2^B$ . [1 mark]

- (c) Write an expression for  $g_1$ . Your answer should be expressed in terms of some (or all) of Z,  $P_1^A$ ,  $P_1^B$ ,  $Q_1^A$ , and  $Q_1^B$ , but none of the period-2 prices or quantities. Simplify your answer as much as possible; note the "some-or-all-of" part of the question. [1 mark]
  - (d) Show how you arrived at your answer under (c). [1 mark]

## Problem 2. Growth Rates and Per-Capita GDP [4 marks]

The table below shows some (incomplete) information about the natural logarithms of two macro variables: total GDP,  $Y_t$ ; and total population,  $L_t$ .

t	$ln(Y_t)$	$\ln(L_t)$
1	1.10	0.90
2	1.10	0.80
3		0.80

Let  $y_t = Y_t/L_t$  denote (non-logged) GDP per capita. Also, let  $g_t^Y = \frac{Y_t - Y_{t-1}}{Y_t}$  denote the net growth rate in  $Y_t$ , with analogous notation for the growth rates of  $y_t$  and  $L_t$ .

- (a) Find the natural logarithm of GDP per capita in period 2,  $ln(y_2)$ . [1 mark]
- (b) Find the (approximate) non-logged GDP per capita in period 2,  $y_2$ . [1 mark]
- (c) Find the (approximate) net growth rate in GDP per capita in period 2,  $g_2^y$ . [1 mark]
- (d) Assume that  $g_3^y = 0.05 = 5\%$ . Find the (approximate) non-logged level of total GDP in period 3,  $Y_3$ . [1 mark]

## Problem 3. Business Cycles [4 marks]

- (a) The diagram provided on the answer sheet shows the time path for the percentage deviation from trend in real GDP. In the same diagram, draw another path showing deviations from trend for some other (imagined) macro variable that is (i) pro-cyclical and (ii) leading the business cycle. Also indicate the trough of the business cycle in the diagram. (There are multiple troughs, but you only need to indicate one.) [2 marks]
- (b) In Canadian data, deviations from trend in GDP have the feature that when it is above trend it is likely to stay above trend, and vice versa when it is below trend. That is, the current deviation is positively correlated with the deviation in the previous period. What we call this feature? Hint: it starts with a P. [1 mark]
- (c) What do we call the most recent recession in Canada? Hint: Two words starting with G and P. [0.5 marks]
- (d) Mention one macro variable that is more variable (or volatile) than GDP in Canadian data. [0.5 marks]
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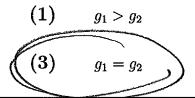
## Econ 2400 Midterm Exam October 6, 2025 - Answer sheet for Problem 1

Version B answers

Student Name:

SID Number:

#### Answer to 1 (a) (circle one):



- $(2) g_1 < g_2$
- (4) Not possible to say

Answer to 1 (b):

#### Answer to 1 (c):

$$GDP_2 = \mathcal{P}_2^A \mathcal{Q}_2^A + \mathcal{P}_2^B \mathcal{Q}_2^B$$

$$g_1 = \mathcal{Z}$$

Answer to 1 (d): (show derivation below)

$$91 = \frac{P_{1}^{A}Q_{2}^{A} + P_{1}^{B}Q_{2}^{A}}{P_{1}^{A}Q_{1}^{A} + P_{1}^{B}Q_{1}^{B}}$$

$$= \frac{P_{1}^{A}ZQ_{1}^{A} + P_{1}^{B}ZQ_{2}^{B}}{P_{1}^{A}Q_{1}^{A} + P_{1}^{B}Q_{2}^{B}}$$

$$= \frac{P_{1}^{A}ZQ_{1}^{A} + P_{1}^{B}Q_{2}^{B}}{P_{1}^{A}Q_{1}^{A} + P_{1}^{B}Q_{1}^{B}} = Z$$

#### Econ 2400 Midterm Exam October 6, 2025 - Answer sheet for Problem 2

Student Name:

SID Number:

Answer to 2 (a):

$$\ln(y_2) = \emptyset$$
, 30

Answer to 2 (b):

$$y_2 = 1.349859$$

Answer to 2 (c):

$$g_2^y = 0.10 = 10\%$$

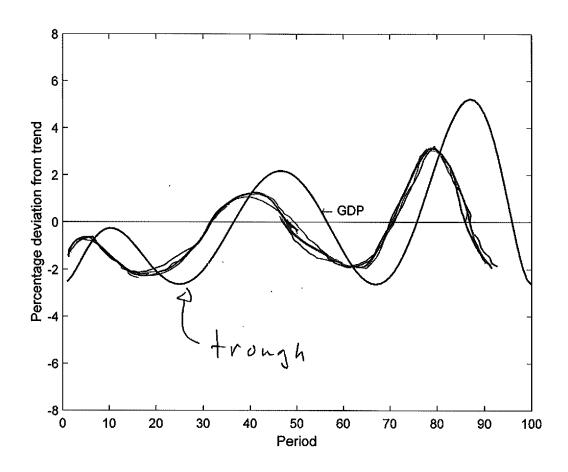
Answer to 2 (d):

$$Y_3 = 3.158193$$

Student Name:

SID Number:

Answer to 3 (a):



Answer to 3 (b):

Answer to 3 (c):

Answer to 3 (d):

Persistence

Global Pandemic

Investment

#### Calculations for Problem 2

#### Version A:

(a)

$$ln(y_2) = ln(Y_2) - ln(L_2) = 1.05 - 0.90 = 0.15$$

(b)

$$y_2 = e^{0.15} \approx 1.161834$$

(c)

$$\ln(y_1) = \ln(Y_1) - \ln(L_1) = 1.00 - 0.80 = 0.20$$
$$g_2^y \approx \ln(y_2) - \ln(y_1) = 0.15 - 0.20 = -0.05 = -5\%$$

(d)

$$g_3^y \approx \ln(y_3) - \ln(y_2) = \ln(y_3) - 0.15 = 0.10$$
  
 $\ln(y_3) \approx 0.10 + 0.15 = 0.25$ 

$$\ln(y_3) = \ln(Y_3) - \ln(L_3) = \ln(Y_3) - 1.00 = 0.25$$
  
 $\ln(Y_3) = 0.25 + 1.00 = 1.25$   
 $Y_3 = e^{1.25} \approx 3.490343$ 

#### Version B:

(a)

$$ln(y_2) = ln(Y_2) - ln(L_2) = 1.10 - 0.80 = 0.30$$

(b)

$$y_2 = e^{0.30} \approx 1.349859$$

(c)

$$\ln(y_1) = \ln(Y_1) - \ln(L_1) = 1.10 - 0.90 = 0.20$$
$$g_2^y \approx \ln(y_2) - \ln(y_1) = 0.30 - 0.20 = 0.10 = 10\%$$

(d)

$$g_3^y \approx \ln(y_3) - \ln(y_2) = \ln(y_3) - 0.30 = 0.05$$
  
 $\ln(y_3) \approx 0.05 + 0.30 = 0.35$ 

$$\ln(y_3) = \ln(Y_3) - \ln(L_3) = \ln(Y_3) - 0.80 = 0.35$$
  

$$\ln(Y_3) = 0.35 + 0.80 = 1.15$$
  

$$Y_3 = e^{1.15} \approx 3.158193$$